# Innovation and Creativity

Computer simulations of effective lattice theories for strongly correlated systems

Steinar Kragset

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Paper I: S. Kragset, A. Sudbø, and F. S. Nogueira, Metal-insulator transition in two- and three-dimensional logarithmic plasmas, Physical Review Letters **92**, 186403 (2004)



Paper I: Metal-insulator transition in two- and three-dimensional logarithmic plasmas

Paper II: K. Børkje, S. Kragset, and A. Sudbø, Instanton correlators and phase transitions in two- and three-dimensional logarithmic plasmas, Physical Review B **71**, 085112 (2005)

Paper I: Metal-insulator transition in two- and three-dimensional logarithmic plasmas

Paper II:

Instanton correlators and phase transitions in two- and three-dimensional logarithmic plasmas

Paper III:

- S. Kragset, E. Smørgrav, J. Hove,
- F. S. Nogueira and A. Sudbø,

First order phase transition in a gauge theory of S = 1/2 quantum antiferromagnets, cond-mat/0609336 (accepted for publication in Physical Review Letters)



Paper I: Metal-insulator transition in two- and three-dimensional logarithmic plasmas

Paper II:

Instanton correlators and phase transitions in two- and three-dimensional logarithmic plasmas

Paper III:

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Paper III: First order phase transition in a gauge theory of S = 1/2quantum antiferromagnets

Paper IV: Thermal fluctuations of vortex matter in trapped Bose–Einstein condensates

Resistance



Temperature T



 — 1911: Superconductivity discovered



- 1911: Superconductivity discovered
- Theory explaining the mechanism in 1957



- 1911: Superconductivitydiscovered
- Theory explaining the mechanism in 1957
- 1986: Discovery of high-temperature superconductors



- 1911: Superconductivitydiscovered
- Theory explaining the mechanism in 1957
- 1986: Discovery of high-temperature superconductors
  - theory still missing

#### **High-temperature superconductors**



#### High-temperature superconductors



#### High-temperature superconductors



- Almost independent 2D planes
- Construct effective lattice models





#### **Effective lattice models**

#### Superconductivity is a macroscopic property

# **Effective lattice models**



- Superconductivity is a macroscopic property
- Simplify microscopic model

Example: Particle description of light

#### **Effective lattice models**



Example: Particle description of light

- Superconductivity is a macroscopic property
- Simplify microscopic model
- Put everything on a lattice

# **Computer simulations**

- Model systems are not physical

# **Computer simulations**

- Model systems are not physical
- Models are simplified, but not that simple

$$\langle 0 
angle = rac{1}{Z} \sum_{\{\psi\}} O_{\psi} \mathrm{e}^{-H_{\psi}/T}$$

# **Computer simulations**

- Model systems are not physical
- Models are simplified, but not that simple

$$\langle 0 
angle = rac{1}{Z} \sum_{\{\psi\}} O_{\psi} \mathrm{e}^{-H_{\psi}/T}$$

- Use computers for experiments

# Computer simulations — Monte Carlo

$$\langle O \rangle = \frac{1}{Z} \sum_{\{\psi\}} O_{\psi} e^{-H_{\psi}/T}$$
 — Statistical methods

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# Computer simulations — Monte Carlo

$$\langle \mathbf{O} 
angle = rac{1}{Z} \sum_{\{\psi\}} \mathbf{O}_{\psi} \mathrm{e}^{-H_{\psi}/T}$$

- Statistical methods
- Temperature enhances fluctuations

# Computer simulations — Monte Carlo

$$\langle 0 \rangle = rac{1}{Z} \sum_{\{\psi\}} O_{\psi} \mathrm{e}^{-H_{\psi}/T}$$



- Statistical methods
- Temperature enhances fluctuations
- Monte Carlo simulations imitate nature's randomness

# Paper I and II: A logarithmically interacting plasma



# Paper I and II: A logarithmically interacting plasma



#### **Dipole moment**

Polarizability proportional to  $\langle s^2 \rangle$ 



#### **Dipole moment**

— Polarizability proportional to  $\langle s^2 \rangle$ 

— Measure  $\langle s^2 \rangle$  as a function of temperature

#### **Dipole moment**

- Polarizability proportional to  $\langle s^2 \rangle$
- Measure  $\langle s^2 \rangle$  as a function of temperature
  - System size upper limit



# Polarizability



#### Inverse dielectric constant



12

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#### Inverse dielectric constant





J. Dalibard

 Some atomic gases condense into superfluids at extremely low temperatures



J. Dalibard

 Some atomic gases condense into superfluids at extremely low temperatures

Does not respond to rotation



J. Dalibard

- Some atomic gases condense into superfluids at extremely low temperatures
- Does not respond to rotation
- Not until a certain rotation rate



J. Dalibard

- Some atomic gases condense into superfluids at extremely low temperatures
- Does not respond to rotation
- Not until a certain rotation rate
- Faster rotation

#### **Vortices**



- Dynamics of neutron stars
- Type-II superconductors
- Rotating Bose condensates and other superfluids

#### **Vortex lattices**



W. Ketterle

- Difficult to control temperature in experiments
- What are the temperature effects?
- Convenient to use Monte Carlo simulations

#### Modelling vortex systems



- Simple model of phase fluctuations



#### Simulated trapped vortex lattices



- Condensate density depletes in outer regions with increasing temperature
- High stability in the lattices

# Conclusions

With Monte Carlo simulations I have studied:

- Phase transitions in effective lattice models for strongly correlated systems
- Thermal fluctuations in trapped Bose-Einstein condensates

The results have been published in four research articles